《有限元法中的数学理论 第2版》

书籍信息

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内容简介

有限元法被广泛用于工程设计和工程分析。本书是Springer出版的《应用数学教材》丛书之15。全书分成15章，在第1版的基础上增加了加性Schwarz预条件和自适应格；书中不但提供有限元法系统的数学理论。还兼重在工程设计和分析中的应用算法效率、程序开发和较难的收敛问题。

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